## What is claimed is:

1. A group III-nitride semiconductor substrate comprising:

a ZrB<sub>2</sub> single crystal base having a defect density of 10<sup>7</sup> cm<sup>-2</sup> or less;

a low-temperature buffer layer consisting of a  $B_xAl_yGa_zIn_{1-x-y-z}N$  ( $0 \le x \le 1$ ,  $0 \le y \le 1$ ,  $0 \le z \le 1$ ,  $0 \le z \le 1$ ,  $0 \le z \le 1$ ) single crystal which is grown or deposited on said  $ZrB_2$  single crystal base substantially without creation of any Zr - B - N amorphous nitrided layer caused by the reaction between a nitrogen atom and said  $ZrB_2$  single crystal base; and

a semiconductor layer consisting of a  $B_aAl_bGa_cIn_{1-a-b-c}N$  ( $0 \le a \le 1$ ,  $0 \le b \le 1$ ,  $0 \le c \le 1$ ,  $0 \le 1-a-b-c \le 1$ ) single crystal grown on said low-temperature buffer layer, said semiconductor layer having an element-forming surface with a dislocation density of  $10^7$  cm<sup>-2</sup> or less in its entirely.

- 2. A semiconductor optical element formed on the semiconductor substrate as defined in claim 1.
- 3. The semiconductor optical element as defined in claim 2, which includes an electrode formed on the side of said base.
- 4. A method of producing a group III-nitride semiconductor substrate, essentially consisting of:

a first step of forming a low-temperature buffer layer consisting of  $B_xAl_yGa_zIn_{1-x-y-z}N$  ( $0 \le x \le 1$ ,  $0 \le y \le 1$ ,  $0 \le z \le 1$ ,  $0 \le 1-x-y-z \le 1$ ), on a  $ZrB_2$  single crystal base having a defect density of  $10^7$  cm<sup>-2</sup> or less, at a base temperature allowing said

low-temperature buffer layer to be grown or deposited on said  $ZrB_2$  single crystal base substantially without creation of any Zr-B-N amorphous nitrided layer; and

a second step of successively to said first step, growing a single crystal film consisting of  $B_aAl_bGa_cIn_{1-a-b-c}N$  ( $0 \le a \le 1$ ,  $0 \le b \le 1$ ,  $0 \le c \le 1$ ,  $0 \le 1-a-b-c \le 1$ ), directly on said low-temperature buffer layer, to form a semiconductor layer consisting of  $Al_aGa_{1-a-b}In_bN$  ( $0 \le a \le 1$ ,  $0 \le b \le 1$ ,  $0 \le 1-a-b \le 1$ ) which has an element-forming surface with a dislocation density of  $10^7$  cm<sup>-2</sup> or less in its entirely.

- 5. The method as defined in claim 4, wherein said low-temperature buffer layer is formed as a single crystal at the time said first step is completed.
- 6. The method as defined in claim 4, wherein said low-temperature buffer layer is polycrystalline or amorphous at the time said first step is completed, and formed as a single-crystal at the time said second step is completed.
- 7. The method as defined in either one of claims 4 to 6, wherein said low-temperature buffer layer has a thickness in the range of 10 nm to 1  $\mu$ m.